

P. 357  
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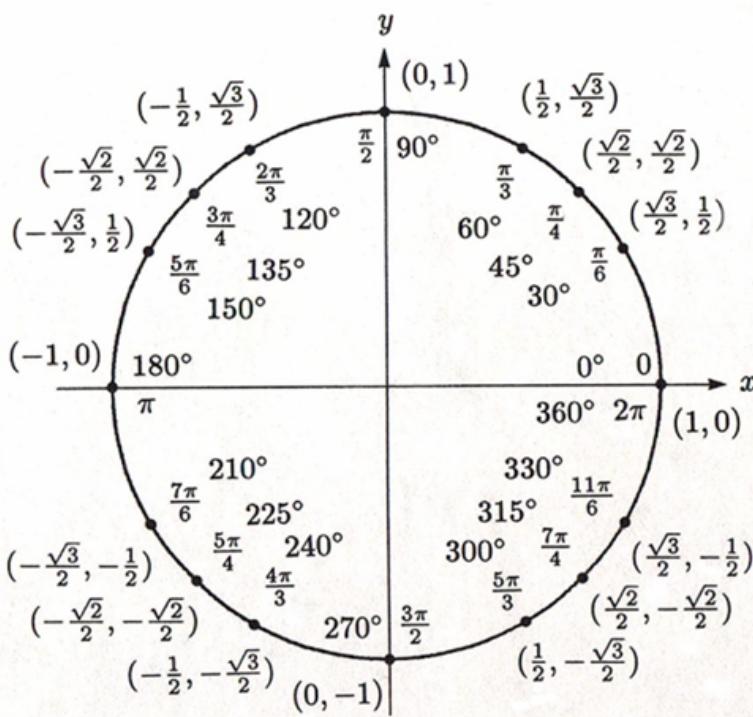
$$\sin\left(\frac{\pi}{2} - x\right) \csc x$$

$$\cos x \csc x$$

$$\frac{\cos x}{1} \cdot \frac{1}{\sin x} = \frac{\cos x}{\sin x}$$

$\cot x$

### 5-3 Solving Trigonometric Equations



Ex 1 Verify that the  $x$ -value is a solution of the equation.

$$\sec x - 2 = 0 \quad x = \frac{\pi}{3}$$

$$\frac{1}{\cos x} - 2$$

Ex.2 Solve for  $x$  in the interval  $[0^\circ, 360^\circ]$   
and in the interval  $[0, 2\pi)$ :

$$\sin x = \frac{\sqrt{3}}{2}$$

Solve

$$x = 60^\circ, 120^\circ$$

$$60^\circ + n \cdot 360^\circ$$

$$120^\circ + n \cdot 360^\circ$$

$$x = \frac{\pi}{3}, \frac{2\pi}{3}$$

$$\frac{\pi}{3} + n \cdot 2\pi$$

$$\frac{2\pi}{3} + n \cdot 2\pi$$

Ex.3 Solve for  $x$  in the interval  $[0, 2\pi)$ :

$$2 \sin x - 1 = 0$$

$$2 \sin x = 1$$

$$\sin x = \frac{1}{2}$$

$$x = \frac{\pi}{6}, \frac{5\pi}{6}$$

Ex.4 Solve for  $x$  in the interval  $[0, 2\pi)$ :

$$3 \tan^2 x - 1 = 0$$

$$3 \tan^2 x = 1$$

$$\sqrt{\tan^2 x} = \sqrt{\frac{1}{3}}$$

$$x = \frac{\pi}{6}, \frac{7\pi}{6}, \frac{5\pi}{6}, \frac{11\pi}{6}$$

$$\tan x = \pm \sqrt{\frac{1}{3}} = \pm \frac{\sqrt{1}}{\sqrt{3}} = \pm \frac{1}{\sqrt{3}}$$

$$\tan x = \pm \frac{1}{\sqrt{3}} = \pm \frac{\sqrt{3}}{3}$$

Ex. 5 Solve for  $x$  in the interval  $[0, 2\pi)$ :

$$4\sin^2 x - 3 = 0$$

$$4\sin^2 x = 3$$

$$\sin^2 x = \frac{3}{4}$$

$$\sin x = \pm \sqrt{\frac{3}{4}} = \pm \frac{\sqrt{3}}{\sqrt{4}} = \pm \frac{\sqrt{3}}{2}$$

$$x = \left\{ \frac{\pi}{3}, \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{5\pi}{3} \right\}$$

Homework

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